Improving Roadmap Quality through Connected Component Expansion

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Abstract

Motion planning is the problem of finding a valid (e.g., collision-free) path through an environment given specified start and goal positions for a moveable object (e.g., a robot), and has applications in fields such as robotics, computer animation [23], computational biology [14], etc. However, it is intractable to use exact algorithms in scenarios involving more than five degrees of freedom (DOFs) [20].

Therefore, sampling-based methods such as Probabilistic RoadMaps (PRMs) [12] and Rapidly-exploring Random Trees (RRTs) [13] are preferred because they compute approximate mappings of the space that can be used to solve problems. These algorithms sacrifice completeness for improved efficiency to scale to many DOF problems. PRMs, in particular, first sample valid configurations from the configuration space ($C_{space}$) [16], the set of all possible (valid and invalid) positions that a robot can take, and then attempt to add valid edges between neighboring configurations with simple local planners (e.g., straight line or others) or deterministic paths. PRMs compute an approximate mapping of the free space producing a roadmap (graph) that may solve queries. Queries are solved by connecting start and goal nodes to the roadmap (if possible), and finding a path (if one exists) using a graph search algorithm. There exist a variety of PRMs, some differing in how they bias node placements and/or edge assignments [1], [25], [24], [22], [6]. All variants, however, still retain the bottleneck of nearest-neighbor queries since each new node is connected to the roadmap. However, some variants have trouble capturing the connectivity of the free space.

In this paper, we present a set of linked-chain expansion methods designed to support PRMs by efficiently improving their roadmap’s connectivity. These methods work by expanding from a selected node in some direction until an obstacle is encountered or reaching a maximum expansion distance, and then repeating the process with a new expansion direction. Expansion nodes are connected to their predecessor and successor nodes without the need for nearest-neighbor queries resulting in chains of connected configurations in the free space. Our first linked-chain method expands in a random direction chosen from a uniform distribution along all DOFs, two others perform goal-biased expansions that explore either towards or away from a particular configuration, respectively, and the fourth grows in both directions tangent to the medial axis.

The primary contributions of this work are as follows:

- Introduction of linked-chain based expansion methods; RandomExpand, ExpandTo, ExpandFrom, and MedialAxisExpand to improve roadmap coverage and connectivity.
- Comparative 2DOF, 6DOF, and 9DOF experiments running PRM, OBPRM, and a hybrid of both, with and without our expansion methods, to show improvements in efficiency in mapping $C_{free}$.

II. RELATED WORK

In this section, we cover the preliminaries of motion planning and describe the most significant related work that is relevant to the proposed methods.
A. Motion Planning Preliminaries

A robot is a movable object whose position and orientation can be described by \( n \) parameters, or degrees of freedom (DOFs), each corresponding to an object component (e.g., position, orientation, link angles, and/or link displacements). Hence, a robot’s configuration \( q \) can be uniquely described by an \( n \)-dimensional vector \( \langle q_1, q_2, \ldots, q_n \rangle \) where \( q_i \) is the \( i \)th DOF. The space, consisting of all possible robot configurations (feasible or not), is called configuration space \( (C_{\text{space}}) \) [16]. The subset of all feasible configurations is the free space \( (C_{\text{free}}) \), while the union of the infeasible configurations is the obstacle space \( (C_{\text{obst}}) \). Thus, the motion planning problem becomes that of finding a continuous trajectory in \( C_{\text{free}} \) from a given start configuration to a goal configuration.

In general, it is intractable to compute explicit \( C_{\text{obst}} \) boundaries [20]. However, the feasibility of configurations can be determined quite efficiently, e.g., by performing a collision detection (CD) test in the workspace, the robot’s natural space, a two or three dimensional space. This motivates the use of sampling-based approaches such as PRMs over exact methods because they only consider a finite set of sampled robot configurations.

B. Probabilistic RoadMaps

The Probabilistic RoadMap [12] algorithms have two major phases as seen below in Algorithm 1: roadmap construction and query. During the construction phase, configurations are sampled in \( C_{\text{space}} \) and validated. This step is followed by a node connection step where deterministic paths between neighboring nodes are computed using nearest-neighbors computations. An optional CC connection step may then be applied, after the node connection step, with varying CC pairing policies to improve the roadmap’s connectivity [17]. Finally, queries are attempted on the roadmap.

Some PRM variants improve sample generation [3], [10], [1], [25], [24], [22], [21]. Obstacle-based PRM, (OBPRM) [1] and Uniform OBPRM (UOBPRM) [25], generate samples near \( C_{\text{obst}} \). Medial-axis based methods [24], [9], [15] generate nodes in areas of high clearance. The Gaussian sampling strategy for PRM [3] and the Bridge Test sampler for PRM [10] both filter node generation to specific areas of the environment, either the boundary of \( C_{\text{obst}} \) or narrow passages respectively.

Making use of node visibility, the Visual PRM (VISPRM) [22] strategy allows for roadmap construction to be concentrated in unexplored areas of \( C_{\text{free}} \). Visibility can also be extended towards considering nodes as representations of hyperspheres in \( C_{\text{free}} \) instead of points [21], and using those volumes to represent regions of configurations as opposed to single configurations. Each of these variants of the original PRM bias their sampling distributions, but may still produce a disjoint roadmap with many connected-components (CCs). The comparative study of PRM variants in [7] goes into further detail in terms of their differences.

Reachability analysis [8] shows that more emphasis needs to be directed towards the connection phase of PRM roadmap construction to improve coverage and connectivity. The metrics described in [18] provide a way to measure the effectiveness of PRM’s to further our understand where these methods perform best. This was extended to improve the sampling process for PRMs by filtering new samples with respect whether they improve roadmap connectivity [19]. The goal of sampling-based approaches to Motion Planning is to approximate \( C_{\text{free}} \) as well as possible. Hence, coverage is an important metric with which we can measure the performance of a method.

Connecting CCs requires a choice of local planners, such as Toggle Local Planner [5], and distance metrics [2]. Some metrics for choosing CC pairings to connect are described in [17] and include size and distance of CC’s as well as others.

Optimal sampling-based methods [11] guarantee that the solution returned by the algorithm is the asymptotically optimal roadmap in terms of shortest paths. PRM*, one such method, is optimal, but suffers from the same bottleneck of nearest-neighbor queries as its sub-optimal variants.

III. Linked-Chain Expansion Methods

Our proposed CC expansion methods are designed to augment PRMs by running immediately after the node connection step and before any subsequent optional CC connection step, where CCs can form because attempted connections between CCs can fail due to the presence of obstacles. By running our methods prior to the CC connection step our methods attempt to improve each CC’s coverage and connection success rate.

Starting from a chosen expansion node, these methods generate a directional ray in \( C_{\text{space}} \) and linearly expand in the given direction until some stopping condition is met, e.g., an obstacle is encountered or a maximum expansion distance
is reached. At which point either a new expansion direction is generated or the expansion ends. The expansion nodes and directions will depend on the chosen biases that will be explained in Sections III-B and III-C, respectively.

Each node in our CC expansion phase can be considered a link in a connected set (usually a chain). Nodes in this set are immediately connected to their predecessor and successor nodes, removing the need for a nearest-neighbor search. Thus, we can avoid nearest-neighbor queries during our expansion process. If multiple CCs exist, these algorithms should increase the likelihood that these CCs will be connectable.

In this section, we will detail the ideas behind CC expansion; first by providing an overview of our CC expansion setup in Section III-A, followed by a description of our node selection process in Section III-B, and a detailed description of each expansion algorithm in Section III-C.

A. Expansion Setup

We present our expansion setup in Algorithm 2. We iterate over every connected component in the roadmap and apply the chosen CC expansion method on the candidate set of expansion nodes.

```
Algorithm 2 General Expansion Scheme
Input: Roadmap $R$, ExpandStrategy $ES$
1: for all $CC \in R$ do
2:     $S \leftarrow$ SelectExpansionNodes($CC$)
3:     for all $s \in S$ do
4:         $ES$.Expand($s$)
```

Many of the algorithms will also make reference to two global input variables $\delta_{\text{min}}$ and $\delta_{\text{max}}$ which provide limits on expansion distances.

1) $\delta_{\text{min}}$ provides a lower-bound for inter-node distances between expansion nodes so that we prune expansions that yield little to no new coverage and to attempt to provide a certain degree of minimal clearance, to each new node, from obstacles (and other nodes in Algorithm 7).
2) $\delta_{\text{max}}$ provides an upper-bound to expansion distances so that we do not produce paths that are too long without intermediate nodes being present.

The expansion framework makes use of the following utility functions:

- $\text{UpdateRoadmap}(q_1, q_2, [q_3])$: This method updates the roadmap by adding node pairs with edges between them. It works by checking if a valid path can be constructed between nodes $(q_1, q_3)$, and if so adds this edge. Else, we add edges $(q_1, q_2)$ and $(q_2, q_3)$. The third argument $[q_3]$ is optional since we may only want to add the pair $(q_1, q_2)$ to the roadmap.
- $\text{ShortDist}(q, r)$ and $\text{LongDist}(q, r)$: These methods return a valid configuration that is at most $\delta_{\text{min}}$ or $\delta_{\text{max}}$ from node $q$ in the direction of ray $r$.

B. Expansion Node Selection Policies

In order to expand roadmap CCs, we first need to identify the candidate nodes in each CC from which to perform the expansion. Since the goal of the expansion process is to increase the connectivity of the roadmap’s CCs, the choice of expansion node becomes an important first step. We want to expand nodes in areas of low visibility and/or node density since these areas may be potential pathways between CCs and would be more likely to provide an increase in coverage. We provide several policies for choosing potential candidate nodes:

1) Random: Picks some random configuration $c \in CC$ for expansion.
2) Farthest: Picks the farthest node from the CC’s centroid using some distance metric (e.g., Euclidean). The centroid represents the configuration with the average of each DOF in the represented CC.
3) Difficult: Makes use of approximate node visibility as its metric [18] by computing the ratio of successful and total connection attempts to each configuration $c \in CC$. The least visible nodes are those with the lowest ratios. We select these as candidates for expansion.

C. Expansion Algorithms

In this section, we describe four expansion algorithms, each of which is a specific derivation of the two-step expansion technique shown in Algorithm 3. The first expansion step performs the expansion in a direction biased towards a suitable goal specific to the method, until an obstacle is reached. The second expansion step acts on the node resulting from the first step and expands in some direction in preparation for the next expansion iteration.
Algorithm 3 Expansion Technique Outline

Input: Node $q$
1: for $i = 1 \ldots Max\text{Iterations}$ do
2: $q' \leftarrow$ FirstExpansion($q$)
3: $q'' \leftarrow$ SecondExpansion($q'$)
4: UpdateRoadmap($q, q', q''$)
5: $q \leftarrow q''$

Algorithm 4 RandomExpand

Input: Node $q$
1: for $i = 1 \ldots Max\text{Iterations}$ do
2: $q' \leftarrow$ LongDist($q, Random\text{Dir}()$)
3: $q'' \leftarrow$ ShortDist($q', Random\text{Dir}()$)
4: UpdateRoadmap($q, q', q''$)
5: $q \leftarrow q''$

1) Random Expand: The first method in the expansion framework, as shown in Algorithm 4 and Figure 1, is the random expansion algorithm. A list of configurations is produced by first performing a long distance expansion in a randomly chosen direction (Fig. 1(a),1(b)), executing a short distance expansion meant to gain some clearance for the next expansion iteration (Fig. 1(c)), and repeating (Fig. 1(d)).

2) Expand-From-CC-Centroid: This method is described in Algorithm 5 and shown in Figure 2. We produce a list of configurations that expand away from the centroid of the node’s CC in the PushAwayFrom(...) step until an obstacle is reached (Fig. 2(a),2(b)), and execute a short expansion in a random direction to gain some clearance for the next iteration, which may help escape local minima (Fig. 2(c)). We continue repeating this process until the max number of iterations is met (Fig. 2(d)).

Algorithm 5 ExpandFrom

Input: Node $q$
1: centroid $\leftarrow$ GetCCCentroid($q$)
2: for $i = 1 \ldots Max\text{Iterations}$ do
3: $q' \leftarrow$ PushAwayFrom($q, centroid$)
4: $q'' \leftarrow$ ShortDist($q', Random\text{Dir}()$)
5: UpdateRoadmap($q, q', q''$)
6: $q \leftarrow q''$

3) Expand-To: Unlike ExpandFrom, Algorithm 6 (example shown in Figure 3) produces a list of configurations as it expands towards the centroid of the nearest neighboring CC using NearestCCCentroid(...) (Fig. 3(a),3(b)), executes a long distance walk in a random direction (Fig. 3(c)), and repeats (Fig. 3(d)). The second expansion step is a long distance instead of a short distance walk because short walks would not provide enough clearance for the proceeding iteration because the algorithm may get stuck expanding into an obstacle.

The algorithm stops when an expansion node is determined to be close enough to that CC’s centroid, as calculated by the WithinProximity(...) subroutine. This method, on line 4 of Algorithm 6, returns true if nodes $n_1$ and $n_2$ are within our predefined distance $\delta_{min}$ from each other and false otherwise.

Note that the number of CCs, and hence the input size of a nearest-neighboring CC computation, is typically much smaller than the number of nodes in the roadmap.

Fig. 1. Example environment (a) shown with a CC (blue) to be expanded. A random vector is chosen and expanded along (b), then a small random directional vector is chosen to push away from obstacles (c). The process is repeated in (d).
(and never more) than the number of configurations. In the event that there is only one CC in the environment, a random direction is selected for expansion instead since there may still be benefit in expanding.

**Algorithm 6 ExpandTo**

**Input:** Node $q$

1. $targetCC \leftarrow \text{NearestCC}_\text{Centroid}(q)$
2. for $i = 1 \ldots \text{MaxIterations}$ do
3. 
4. 
5. 
6. 
7. 
8. 
9. 
10. $q \leftarrow q''$

4) **Medial-Axis Expand:** Unlike the previous methods, our final expansion strategy, as seen in Algorithm 7 and Figure 4, biases expansion along the medial axis. This method requires a history of the previous two expansion nodes, so we initialize this history by shooting a ray in a random direction from our initial expansion node $q$ until we impact an obstacle or reach max distance $\delta_{\text{max}}$, where we place a valid (non-colliding) “bump” node $q'$ (Fig. 4(a), 4(b)). We push $q'$ to the medial-axis and place a second temporary node $q''$ (Fig. 4(c)). After running UpdateRoadmap(..), we recursively expand in both directions of the tangent (lines 10 and 14 of Algorithm 7), and repeat (Fig. 4(d)).

The IsClear(..) method, on lines 7 and 11 of Algorithm 7, is a method designed to make sure that we do not expand into areas already mapped by other expansion branches by making sure that each new medial-axis nodes is at least $\delta_{\text{min}}$ distance away from all the others. This is meant to prune expansion branches that are expected to garner little-to-no gain in coverage.

Note that we check to see if we are currently in iteration zero since our first random expansion may produce initial nodes that are too close and may trigger the IsClear(..) condition to return false.

Algorithm 8 uses two cross products to produce a ray $\vec{c}_2$ tangent to the medial-axis at node $q''$. We only use the robot’s positional degrees of freedom when computing the tangent rays since using rotational DOFs would cause us to return rays that do not reflect the medial-axis of the workspace and may produce trajectories into obstacles.
Algorithm 7 MedialAxisExpand

**Input:** Node $q$, Ray $r$, Int $i$

1. if $i > \text{MaxIterations}$ then
2. return
3. $q'_1 \leftarrow \text{LongDist}(q, r)$
4. $q'_2 \leftarrow \text{LongDist}(q, -r)$
5. $q''_1 \leftarrow \text{PushToMedialAxis}(q'_1)$
6. $q''_2 \leftarrow \text{PushToMedialAxis}(q'_2)$
7. if $\text{IsClear}(q''_1) \&\& i \neq 0$ then
8. $\text{UpdateRoadmap}(q, q'_1, q''_1)$
9. $r' \leftarrow \text{MedialAxisTangent}(q, q'_1, q''_1)$
10. $\text{MedialAxisExpand}(q''_1, r', i + 1)$
11. if $\text{IsClear}(q''_2) \&\& i \neq 0$ then
12. $\text{UpdateRoadmap}(q, q'_2, q''_2)$
13. $r' \leftarrow \text{MedialAxisTangent}(q, q'_2, q''_2)$
14. $\text{MedialAxisExpand}(q''_2, r', i + 1)$

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![Fig. 4](image_url)

Fig. 4. Example environment (a) shown with a CC (blue) to be expanded with bias along the medial axis (dotted gray line). A direction is chosen to expand along (b), and then this node is pushed towards the medial axis (c). Finally, a vector combination of the dotted red lines (from the previous expansions) is used to expand along both directions of the tangent of the medial axis (d).

IV. EXPERIMENTS AND RESULTS

In this section, we perform a case study of six environments of varying topologies and difficulties. The experiments aim to compare PRM, OBPRM, and the Hybrid (PRM/OBPRM) method with and without a CC expansion step. The experiments compare the efficiency in mapping $C_{\text{free}}$.

A. Experimental Setup

All experiments were run on a Rocks Cluster running CentOS 5.1 with Intel XEON CPU 2.4 GHz processors with the GNU gcc compiler version 4.1.2.

All the PRM variants and expansion methods described in this paper were implemented in a C++ library developed in the Parasol Lab at Texas A&M University. It uses a distributed graph data structure from the Standard Template Adaptive Parallel Library (STAPL) [4], a C++ library designed for parallel computing. Samples are generated with uniform (PRM), obstacle-based (OBPRM), mixed (Hybrid) distributions.

To connect nodes, a euclidean distance metric is used with a straight-line local planner. Each of our sampler’s continuously sampled 50 nodes before running our CC expansion methods each iteration until our goal of 90% approximate roadmap connectivity was achieved. We attempted to expand from two expansion nodes per CC for seven expansion iterations in all cases involving CC expansion. Our stopping condition made use of a sample query of over 100 nodes, that were uniformly sampled from each environment, as a representative set for $C_{\text{free}}$. After each iteration, we attempted queries between all

Algorithm 8 MedialAxisTangent

**Input:** Nodes $q, q', q''$

1. $\vec{a} = (q, q')$
2. $\vec{b} = (q', q'')$
3. $\vec{c}_1 = \vec{a} \times \vec{b}$
4. $\vec{c}_2 = \vec{b} \times \vec{c}_1$
5. return $\vec{c}_2$
pairs of these nodes using the current roadmap and computed the approximate connectivity as the ratio between successful and total number of query attempts.

All run time results have been normalized such that all PRM results are normalized to the Basic PRM method, similarly the OBPRM and Hybrid experiments have normalize each of the plots in Sections IV-B, IV-C, and IV-D abide by the legend in Fig. 8: The x-axes of these plots will also make use of the keys in Table I to denote CC expansion method and node selection policy combinations. The “BASIC” label will be applied to experiments where PRM, OBPRM, or Hybrid do not include any expansion methods. Otherwise, the following keys will be used to refer to method combinations where the first two letters denote the expansion method and the third letter, after the hyphen, refers to the node selection policy.

Six environments were used in our experiments: three 2DOF, two 6DOF, one 9DOF as displayed in Fig. 5, 6, and 7 respectively.

Fig. 5. Environment (a) is our simple tunnel (s-tunnel) environment with two open areas and one narrow passage. Our cluttered environment is (b) with 250 square obstacles. The maze environment (c) contains many long narrow passages and two entrances. In each of our 2DOF environments, we use a 2DOF translational robot.

Fig. 6. Both of our 6DOF environments provide narrow passages. The U-Tunnel (a) has several curved passages with with four entrances, two on the top and bottom. The Z-Tunnel (b) has a series of straight inter-connected tunnels that zigzags through the interior of the rectangular box (we’ve removed the ceiling to reveal the tunnel in the above image). In each of our 6DOF environments, we use a 6DOF rectangular box robot.

Fig. 7. Our Heterogeneous environment was used in our 4-link 9DOF robot experiments, it consists of a box with a narrow passage with a cluttered region followed by open space at both openings of the narrow passage.

Fig. 8.

B. 2DOF - Experimental Results

1) S-Tunnel Environment: The S-Tunnel environment is shown in Fig. 9. We show that when our expansion methods are applied, there is a decrease in total mapping time in most PRM experiments. Choosing the Difficult nodes was the best choice since they were more likely to be within the narrow passages, thus expansion were more likely to improve CC coverage the narrow passage. The Random and Farthest node selection policies were more likely to select nodes for
expansion that were less likely to yield reductions in the total mapping time. When attempting to expand in narrow passages, it is not beneficial to pick random nodes to expand from since it is not likely they will be in the narrow passage. Choosing the Farthest nodes will not help either due to the random structure that CCs can take, making the Farthest node(s) a poor choice. Since OBPRM managed to place more nodes in the narrow passage, forming CCs in the narrow passage, we see significant improvement in all method combinations. The Hybrid experiments also reflected this pattern, in all cases, since the OBPRM nodes placed in the narrow passage allowed the expansion methods, regardless of node selection policy, to map it.

### Table I

<table>
<thead>
<tr>
<th>Node Type</th>
<th>RandomExpand</th>
<th>ExpandTo</th>
<th>ExpandFrom</th>
<th>MedialAxisExpand</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random Node</td>
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<td>ET-R</td>
<td>EF-R</td>
<td>MA-R</td>
</tr>
<tr>
<td>Farthest Node</td>
<td>RE-F</td>
<td>ET-F</td>
<td>EF-F</td>
<td>MA-F</td>
</tr>
<tr>
<td>Difficult Node</td>
<td>RE-D</td>
<td>ET-D</td>
<td>EF-D</td>
<td>MA-D</td>
</tr>
</tbody>
</table>

#### 2) Clutter Environment:

The Clutter environment is shown in Fig. 10. The large number of obstacles produce many narrow passage areas that needed to be navigated to connect CCs. The PRM experiments show and improvement the majority of experiments, the best improvement came from MedialAxisExpand with a 25% improvement in total mapping time since the expansions along the medial-axis expanded each CC’s coverage much quicker than the other methods. The OBPRM and Hybrid experiments followed this pattern, though we saw improvement beyond 50% during the OBPRM experiments when using MedialAxisExpand.

![Experiments in the Clutter Environment](image)

#### 3) Maze Environment:

The Maze environment is shown in Fig. 11. The Maze contains many long narrow passages; we see that MedialAxisExpand mapped $C_{free}$ very quickly with ExpandFrom close behind. ExpandFrom worked well because when expanding away from a CC’s centroid in straight narrow passages, the nodes could be placed at the ends of the passages allowing other CCs to possibly connect to them. ExpandTo, using Random node selection, returned the lowest gain and sometimes increased the running time because very few expansion attempts would yield any benefits since a thin

![Experiments in the Maze Environment](image)
wall separating two CCs may cause the CCs to attempt to expand into each other. Notice that ExpandTo also produced a 
large outlier when using the Random node selection policy. This was because choosing to expand to the nearest CC from 
a random node would fail very often.

C. 6DOF - Experimental Results

1) U-Tunnel Environment: The U-Tunnel environment is shown in Fig. 6(a). In the U-Tunnel, we see that only the 
MedialAxisExpand strategy provided a significant performance increase. In higher dimensions, RandomExpand is not likely 
to yield benefit in narrow passages. The ExpandFrom and ExpandTo methods would be trapped in local minima produced 
by the curved nature of the narrow passages, so the potential benefit of their secondary expansion steps, meant to increase 
clearance, would not be of much benefit.

D. 9DOF - Experimental Results

1) Heterogeneous Environment: The 9DOF Heterogeneous environment is shown in Fig. 7. For our articulated-linkage 
experiments, we used a complex environment with two cluttered regions with a narrow passage separating them. The best 
expansion strategy was ExpandFrom, across all methods, because it would expand well through the narrow passage and 
around obstacles allowing both halves of the environment to be connected. The best node selection strategy was the Farthest 
node policy. Expanding from Random nodes would yield little benefit in this environment.
E. Discussion

From our experiments we have noticed that each of our expansion methods and node selection policies are best applied in certain domains. RandomExpand works in most cases. In higher dimensions the benefits are lessened. ExpandFrom works well, even at higher dimensions and with articulated-linkage robots if narrow passages are not curved. ExpandTo worked similarly to ExpandFrom, however, in maze-like environments this method increased the total mapping time. MedialAxisExpand was the best expansion strategy in almost every case since expansions were always performed along the medial-axis guaranteeing that each expansion step would produce long edges that may map difficult regions, especially narrow passages since the expansion is performed along both directions of the medial-axis.

With respect to the node selection policies, the Farthest node policy was best suited to narrow passage problems and the Difficult node policy was suited cluttered environments. The Random node policy performed poorly in many cases when compared to the other two strategies; this is understandable since expanding from a random node in a large roadmap is unlikely to yield much benefit.

V. Conclusion

In this paper, we present a set of novel linked-chain expansion methods, and results from a study of their performance in various 2DOF, 6DOF, and 9DOF environments when compared against PRM, OBPRM, and a Hybrid of both. These linked-chain expansion methods focus expansion in different ways to increase the visibility of connected components and improve roadmap coverage and connectivity. We experimentally show that in environments of varying complexity that our methods tend to improve roadmap connectivity quicker than PRM and OBPRM alone when the expansion bias and node selection policy compliments the environment’s geometry. In more complicated scenarios, the performance of our methods become more specialized showing that different problem types call for specific expansion strategies.

In the future, we want to further explore the efficiency of these methods to improve roadmap connectivity in higher dimensions. Exploring higher dimensional problems would allow us to further analyze the benefits expansion method biases and node selection methods.
REFERENCES


