

An Efficient Static Trace Simplification Technique for Debugging Concurrent Programs

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Abstract. One of the major difficulties in debugging concurrent programs is that the programmer usually experiences frequent thread context switches, which perplexes the reasoning process. This problem can be alleviated by trace simplification techniques, which produce the same computation process but with much fewer number of context switches. The state of the art trace simplification technique takes a dynamic approach and does not scale well to large traces, hampering its practicality. We present a static trace simplification approach, *SimTrace*, that dramatically improves the efficiency of trace simplification through reasoning about the computation equivalence of traces offline. By constructing a dependence graph model of events, our trace simplification algorithm scales linearly to the trace size and quadratic to the number of nodes in the dependence graph. Underpinned by a trace equivalence theorem, we guarantee that the results generated by *SimTrace* are sound and no dynamic program re-execution is required to validate the trace equivalence. Our experiments show that *SimTrace* scales well to traces with more than 1M events, making it attractive to practical use.

Keywords: Trace simplification, Debugging, Concurrent program

1 Introduction

Software is becoming increasingly concurrent due to the prevalence of multicore hardware. Unfortunately, the unique non-deterministic nature of concurrency makes debugging concurrent programs notoriously difficult. For instance, according to a recent report [8], the average bug fixing time of concurrency bugs (137 days) is 2.58 times longer than that of sequential ones in the MySQL¹ project. In our experience, the challenge of debugging concurrent programs comes from two main sources. First, concurrency bugs are hard to reproduce, as they may only manifest under certain specific thread interleavings. Due to the non-deterministic thread interleavings, a concurrency bug manifested in an earlier execution may “disappear” when the programmer attempts to reproduce it [16]. Second, concurrency bugs are hard to understand. A buggy concurrent program execution often contains many thread context switches. Since most programmers are used

¹ <http://www.mysql.com/>

to thinking sequentially, they have to jump frequently from the context of one thread to another for reasoning about a concurrent program execution trace. These frequent “context switches” of the programmers’ minds significantly impair the efficiency of debugging concurrent programs [13].

Researchers have studied the first problem for several decades [5] and numerous effective approaches [11, 15, 19, 18, 12] are proposed for reproducing concurrency bugs. For the second problem, Jalbert and Sen [13] have recently proposed a *dynamic* trace simplification technique, *Tinertia*, for reducing the number of thread interleavings in a buggy execution trace. From a high level perspective, *Tinertia* iteratively transforms an input trace that satisfies a certain property to another trace satisfying the same property but with smaller number of thread context switches. *Tinertia* is valuable in improving the debugging efficiency of concurrent programs as it prolongs the sequential reasoning of concurrent program executions and reduces frequent “context switches”. However, since *Tinertia* is a dynamic approach, it faces serious efficiency problems when used in practice. To reduce every single context switch, *Tinertia* has to re-execute the program at least once to validate the equivalence of the transformed trace. It is very hard for *Tinertia* to scale to large traces as the program re-execution typically requires controlling the thread scheduler to follow the scheduling decisions in the transformed trace, which is often 5x to 100x slower than the native execution [19]. From the time complexity point of view, the total running time of *Tinertia* is cubic to the trace size [13].

In this paper, we present a *static* trace simplification technique, *SimTrace*, that dramatically improves the efficiency of trace simplification through the offline reasoning of the computation equivalence of traces. The key idea of *SimTrace* is that we can statically guarantee the trace equivalence by leveraging the dependence relations between events in the trace. By presenting a formal modeling of dependence relation, we show a theorem of trace equivalence that any rescheduling of the events in the trace respecting the dependence relation is equivalent to the given trace. The trace equivalence is not limited to any specific property but general to all properties that can be defined over the program state. Underpinned by the trace equivalence theorem, *SimTrace* is able to perform the trace simplification completely offline, without any dynamic re-execution to validate the intermediate simplification result, which significantly improves the efficiency of the trace simplification.

In our analysis, we first build a *dependence graph* that encodes all the dependence relations between events in the trace. The dependence graph is a direct acyclic graph in which each node in the graph represents a corresponding event or event sequence by the same thread in the trace, and each edge represents a data dependence or partial order relation between two events or event sequences. The dependence graph is sound in that it encodes a complete set of dependence relations between the events. And the trace equivalence theorem guarantees that any topological sort of the dependence graph produces an equivalent trace to the original trace.

Taking the advantage of the dependence graph, we reduce the trace simplification problem to a *graph merging problem*, of which the objective is minimizing the size of the graph. To address this problem, we developed a graph merging algorithm that performs a sequence of merging operations on the graph. Each merging operation is applied on two consecutive nodes by the same thread in the graph, and it consolidates the two nodes if a merging condition is satisfied. The merging condition is that the edge connecting the two merged nodes is the only path connecting them in the graph, which can be efficiently checked by computing the reachability relation between the two nodes.

Finally, `SimTrace` performs a topological sort on the reduced dependence graph and generates the simplified trace. The total running time of `SimTrace` is linear in the size of the trace and quadratic in the number of the nodes in the initial dependence graph. `SimTrace` is very efficient in practice, since the size of the initial dependence graph is often much smaller than that of the original trace. Moreover, guaranteed by the sound dependence graph model, `SimTrace` is completely static and does not require any re-execution of the program for validating the equivalence of the simplified trace.

For the general trace simplification problem of generating equivalent traces with *minimum* context switches, Jalbert and Sen [13] have proved that this problem is NP-hard and there is unlikely an efficient algorithm for solving it in polynomial time. Like `Tinertia`, `SimTrace` does not guarantee the globally optimal simplification but a local optimum. However, our evaluation results using a set of multithreaded programs show that `SimTrace` has good performance that is able to significantly reduce the context switches in the trace. For instance, for the input trace of the *Cache4j* subject with 1,225,167 events, `SimTrace` is able to reduce the number of context switches from 417 to 33 (with 92% reduction percentage) in 592 seconds. The overall reduction percentage of `SimTrace` ranges from 65% to 97% in our experiments.

Being a static analysis technique, `SimTrace` is complementary to `Tinertia`. For the sake of efficiency, our modeling of the dependence relation does not consider the runtime value dependencies between events in the trace and hence may be too strict in preventing further trace simplification. As `Tinertia` utilizes the runtime verification regardless of the dependence relation, it might be able to explore more simplification opportunities that are beyond the strict dependence relation. A good match between `SimTrace` and `Tinertia` for the trace simplification is to apply `SimTrace` as a front-end and use `Tinertia` as a back end. By working together, we can achieve both the trace simplification efficiency and effectiveness at the same time, i.e., to more efficiently generate a simplified trace with fewer context switches.

To sum up, the key contributions of this paper are as follows:

- We present an efficient static trace simplification technique for reducing the number of thread context switches in the trace.
- We show a theorem of trace equivalence that is general to all properties defined over the program state. This theorem provides the correctness guar-

antee of the static trace simplification without any dynamic program re-execution to validate the intermediate simplification result.

- We present a sound graph modeling of the dependence relation between events in the trace, which allows us to develop efficient graph merging algorithms for the trace simplification problem.
- We evaluate our approach on a number of multithreaded applications and the results demonstrate the efficiency and the effectiveness of our approach.

The rest of the paper is organized as follows: Section 2 describes the problem of trace simplification; Section 3 presents our algorithm; Section 4 reports our evaluation results; Section 5 discusses the related work and Section 6 concludes this paper.

2 Preliminaries

In this section, we first describe a simple but general concurrent program execution model. Based on this model, we then formally introduce the general trace simplification problem.

2.1 Concurrent program execution model

To formally present the trace simplification problem and to prove the trace equivalence theorem, we need to define a concurrent program execution model with precise execution semantics. Previous work [7, 6, 23] has described the concurrent program execution models in several different ways for different analysis purposes. To make our approach general, we define a model in a similar style to [7].

A concurrent program in our language consists of a set of concurrently executing threads $\mathbb{T} = \{t_1, t_2, \dots\}$ that communicate through a global store σ . The global store consists of a set of variables $\mathbb{S} = \{s_1, s_2, \dots\}$ that are shared among threads. Each thread has also its own local store π , consisting of the local variables and the program counter to the thread. We use $\sigma[s]$ to denote the value of the shared variable s on the global store. Each thread executes by performing a sequence of actions each of which operates on a single variable on the global store or the thread's own local store. Let $var(\alpha)$ denote the variable accessed by α . If $var(\alpha)$ is a shared variable, we call α a *global action*, otherwise it is a *local action*. Since the program counter is included in the local store, each thread is deterministic and the next action of t_i is determined by t_i 's current local store π_i . The program state is defined as $\Sigma = (\sigma, \Pi)$, where σ is the global store and Π is a mapping from thread identifiers t_i to the local store π_i of each thread.

The program execution is modeled as a sequence of transitions defined over the program state Σ . Let α^k be the k^{th} action in the global order of the program execution and Σ^{k-1} be the program state just before α^k is performed (Σ^0 is the initial state), the state transition sequence is:

$$\Sigma^0 \xrightarrow{\alpha^1} \Sigma^1 \xrightarrow{\alpha^2} \Sigma^2 \xrightarrow{\alpha^3} \dots$$

Given a concurrent system described above, the execution semantics of actions are defined as follows:

Local action When a local action is performed by a thread, only the local store of that thread is changed to a new state determined by its current state. The global store and the local stores of the other threads remain the same.

Global action When a global action is performed by a thread t_i on the shared variable s , only s and π_i are changed to new states. The states of all the other shared variables on the global store as well as the local stores of all the other threads remain the same. To make the execution model general to different programming languages, we consider the following types of global actions:

- READ - a thread reads the value of a shared variable in the global store into its local store;
- WRITE - a thread assigns some value to a shared variable in the global store;
- LOCK - a thread acquires a lock;
- UNLOCK - a thread releases a lock;
- FORK - a thread forks a new thread;
- JOIN - a thread joins the termination of another thread;
- START - a *dummy* action indicating that a thread is ready to run;
- EXIT - the last action of a thread;
- SIGNAL - a thread sets the value of a conditional variable to 1;
- WAIT - a thread waits for a conditional variable to become 1 and resets it back to 0 after it becomes 1.

It is important notice that, for any action, either a global action or a local action, it only *operates on a single variable*. This is also true for synchronization actions, though they are only enabled when certain pre-conditions are met.

2.2 General trace simplification problem

Definition 1. A *trace* is the action sequence $\langle \alpha^k \rangle$ of a program execution.

Definition 2. A **context switch** occurs when two consecutive actions in the trace are performed by different threads.

Let $\Gamma(\alpha)$ denotes the owner thread of action α . Let δ denote a trace containing N actions and $\delta[k]$ the k^{th} action in δ , and let $CS(\delta)$ denote the number of context switches in δ , we have $CS(\delta) = \sum_{k=1}^{N-1} u_k$ where u_k is a binary variable s.t. $u_k = 1$ if $\Gamma(\delta[k]) \neq \Gamma(\delta[k+1])$ and $u_k = 0$ otherwise.

Definition 3. Two traces are **equivalent** if they drive the same initial program state to the same final program state.

Given a trace as the input, the general trace simplification problem is to produce an output trace that is *equivalent* to the input trace and has minimum number of context switches among all the equivalent traces. To state more formally, suppose an input trace δ drives the program state to Σ^N , the general

trace simplification problem is: *given δ , output a δ' s.t. $\Sigma^N = \Sigma'^N$ and $CS(\delta')$ is minimized.* Notice that the program state here is not limited to any local store or the global store but includes both the global store and the local stores of all the threads. In other words, the trace simplification problem defined above is general to all properties defined over the program state.

The basic idea for reducing the context switches in a trace is to reschedule the actions in the trace such that more actions by the same thread are placed next to each other. A naive approach is to exhaustively generate all permutations of the events in the trace and pick an equivalent one with the smallest number of context switches. However, this naive approach requires checking $N!$ permutations which is highly inefficient. A better approach is to repeatedly move the interleaving actions to some non-interleaving positions and then consolidate the neighboring actions by the same thread. However, there are two major challenges in this approach. First, how to ensure the rescheduled trace is feasible and also equivalent to the input trace? Second, how to make sure the output trace is optimal, i.e., has the minimum number of context switches among all the equivalent traces?

3 SimTrace: Efficient Static Trace Simplification

We address the trace simplification problem by leveraging the dependence relationship between actions in the trace. For the first challenge, we show that the trace equivalence can be guaranteed by respecting the dependence relation during the rescheduling process. For the second challenge, since Jalbert and Sen [13] have proved it is *NP-hard*, we present an efficient algorithm, **SimTrace**, that guarantees to generate a locally optimal solution. In this section, we first describe our modeling of the dependence relation. Based on the modeling, we describe a theorem of trace equivalence and offer a detailed proof. After that, we present the full **SimTrace** algorithm.

3.1 Modeling of the dependence relation

Previous work has proposed many causal models [20, 3, 14, 17, 25] that characterize the dependence relationship between actions in the trace. Among them, most models are developed for checking concurrency properties such as data race and atomicity violations, and they are tailored for the specific property. Different from these models, as we are dealing with all properties over the program state, we have to consider a general model that works for all properties.

Moreover, to support efficient trace simplification, the model should be as simple as possible. Although using a more precise dependence relation model, such as the maximal causal model [20] or the guarded independence model [25], may give us more freedom to simplify the trace (which can further reduce the context switches), such a model is often very expensive to construct in practice, because it requires to track all the value dependencies between events along the program branches and all the correlated control flow decisions in the program execution. We thus use a strict model defined as follows:

Definition 4. The **dependence relation** (\rightarrow) for a trace δ is the smallest transitive closure over the actions in δ , such that $a_i \rightarrow a_j$ holds whenever a_i occurs before a_j and one of the following holds:

- **Local dependence relation**
 - *Program order* - a_i immediately precedes a_j in the same thread.
- **Remote dependence relation**
 - *Synchronization order* - a_i and a_j are consecutive synchronization actions by different threads on the same shared variable. There are four types of synchronization orders:
 - * UNLOCK \rightarrow LOCK: a_i is the UNLOCK action that releases the lock acquired by the LOCK action a_j ;
 - * FORK \rightarrow START: a_i is the FORK action that forks the thread whose START action is a_j ;
 - * EXIT \rightarrow JOIN: a_i is the EXIT action of a thread that the JOIN action a_j joins;
 - * NOTIFY \rightarrow WAIT: a_i is the NOTIFY action that sets the conditional variable the WAIT action a_j waits for;
 - *Conflicting order* - a_i and a_j are consecutive conflicting actions by different threads on the shared variable. There are three types of conflicting orders:
 - * WRITE \rightarrow READ: a_i is a WRITE action and a_j is a READ action;
 - * READ \rightarrow WRITE: a_i is a READ action and a_j is a WRITE action;
 - * WRITE \rightarrow WRITE: both a_i and a_j are WRITE actions.

Given a dependence relation $a_i \rightarrow a_j$, If a_i and a_j are from different threads, we say a_i has a remote outgoing dependence to a_j , and similarly, a_j has a remote incoming dependence to a_i ; Otherwise, we say a_i has a local outgoing dependence to a_j and a_j has a local incoming dependence to a_i .

It is important to notice that the remote dependence relations in our model are all between actions accessing the same shared variable. Therefore, context switches between threads accessing different variables in the trace are allowed to be reduced in our model. Nevertheless, also note that the remote dependence in our modeling includes both the synchronization order and the conflicting order, which may actually be unnecessary if we consider the value dependencies between events. For example, two writes to the same variable with the same value can be permuted without affecting the correctness of the trace. The main purpose for using this strict model is that we want to efficiently and safely guarantee the trace equivalence, towards which we must ensure that every action in the simplified trace reads or writes the same value as its corresponding action in the original trace.

3.2 A theorem of trace equivalence

Based on our model of the dependence relation in Section 3.1, we have the following theorem of trace equivalence:

Theorem 1. *Any rescheduling of the actions in a trace respecting the dependence relation defined in Definition 4 generates an equivalent trace.*

Proof. (Sketch) Let δ denote the input trace with size N and δ' an arbitrary rescheduling of δ respecting the dependence relation, and suppose δ and δ' drive the program state from the same initial state Σ^0 and Σ'^0 to Σ^N and Σ'^N , respectively. Our goal is to prove $\Sigma'^N = \Sigma^N$. The main insight of the proof is that, by respecting the order defined by the dependence relation, every action in the rescheduled trace reads or writes the same value on the program state as its corresponding action in the input trace, and hence the rescheduled trace drives the program to the same final state as that of the input trace. We provide the full detailed proof in the Appendix A. Readers may skip it at this moment. ■

Note that Theorem 1 is related to but different from the equivalence axiom of the Mazurkiewicz traces [1] in the trace theory, which provides an abstract model of reasoning about trace equivalence based on the partial order relation between events. We prove Theorem 1 in the context of concurrent program execution based on the concrete modeling of the action semantics and the computation effect in the trace.

In spite of the intuitiveness, Theorem 1 forms the basis of static trace simplification as it guarantees every rescheduling of the actions in the trace that respects the dependence relation produces a valid simplification result, without the need of any runtime verification. In other words, as long as we do not violate the order defined by the dependence relation, we can safely reschedule the events in the trace without worrying about correctness of the final result.

3.3 SimTrace algorithm

Our algorithm starts by constructing from the input trace a dependence graph (see Definition 5), which encodes all the actions in the trace as well as the dependence relations between the actions. We then simplify the dependence graph by ordinally performing a “merging” operation on two consecutive nodes by the same thread in the graph. When the dependence graph cannot be further simplified, our approach applies a simple topological sort on the graph to produce the final simplified trace.

Definition 5. *A dependence graph $G = (V, E)$, built upon a trace, is a directed acyclic graph in which each $v \in V$ corresponds to a sequence of consecutive actions by the same thread started by a unique action that has remote incoming dependence. For each edge, there is a labeling relation $L : E \rightarrow \{\text{local}, \text{remote}\}$ such that each local edge connects neighboring nodes by the same thread, and each remote edge connects nodes by different threads meaning that there are dependence relations from some actions in one node to some actions in the other node.*

Note that the dependence graph is directed acyclic graph. Otherwise it indicates there are cyclic dependences between events in the trace, which is impossible according to dependence relation model. We next describe our algorithms for constructing and simplifying the dependence graph in detail.

Algorithm 1 ConstructDependenceGraph(δ)

```
1: input:  $\delta$  (a trace)
2: output: graph (the dependence graph built from  $\delta$ )
3:  $map_{t2n} \leftarrow$  empty map from a thread identifier to its current graph node
4:  $t_{old} \leftarrow$  null
5: for  $i \leftarrow 0$  to  $|\delta|-1$  do
6:    $t_{cur} \leftarrow$  the thread identifier of the action  $\delta[i]$ 
7:    $node_{cur} \leftarrow map_{t2n}(t_{cur})$ 
8:   if  $node_{cur}$  is null then
9:      $node_{cur} \leftarrow$  new node( $\delta[i]$ )
10:     $map_{t2n}(t_{cur}) \leftarrow node_{cur}$ 
11:    add node  $node_{cur}$  to graph
12:   else
13:     if  $\delta[i]$  has remote incoming dependence and  $t_{cur} \neq t_{old}$  then
14:        $node_{old} \leftarrow node_{cur}$ 
15:        $node_{cur} \leftarrow$  new node( $\delta[i]$ )
16:       add node  $node_{cur}$  to graph
17:       add local edge  $node_{old} \rightarrow node_{cur}$  to graph
18:       for each action  $a$  with remote outgoing dependence to  $\delta[i]$  do
19:          $node_a \leftarrow$  the node to which  $a$  belongs
20:         add remote edge  $node_a \rightarrow node_{cur}$  to graph
21:       end for
22:     else
23:       add action  $\delta[i]$  to  $node_{cur}$ 
24:     end if
25:   end if
26:    $t_{old} \leftarrow t_{cur}$ 
27: end for
```

Dependence Graph Construction Algorithm 1 shows our algorithm for constructing the dependence graph. Given an input trace, we first conduct a linear scan of all the actions in the trace to build the smallest dependence relation between actions, according to our model in Section 3.1. We then visit each action in their appearing order in the trace once to construct the dependence graph according to Definition 5. Our construction of the dependence graph leverages the observation that most of the dependence relations in the trace are local dependencies within the same thread, while the number of remote dependence relations are comparatively much smaller. We can hence greatly reduce the size of the initial dependence graph by shrinking consecutive actions with only local dependence between them into a single node. The running time of Algorithm 1 is linear to the trace size.

Note that, in our dependence graph construction process, each node in the initial dependence graph has exactly two incoming edges except the root node: a local incoming edge and a remote incoming edge. The number of edges in the graph is thus less than twice the number of nodes in the graph. Moreover, since each node in the dependence graph may represent a sequence of actions in the trace, the number of nodes in the graph is much smaller than the original trace

size. As a result, performing a topological sort on the dependence graph is much more efficient than that on the original trace.

Simplifying Dependence Graph Following Theorem 1, it is easy to see that any topological sort of the initial dependence graph produces a correct answer to our problem, i.e., generates an equivalent trace to the input trace. However, to make the resultant trace as simple as possible, i.e., to minimize the context switches, we have to wisely choose the next node in each sorting step during the topological sort, which is a difficult problem with no existing solution or even good approximation algorithm, to our best knowledge.

We formulate this problem as an optimization problem on the number of nodes in the dependence graph and use a graph merging algorithm to compute a locally optimal solution to it. Before describing the formulation, let us first introduce a dual notion of context switch:

Definition 6. *A context continuation occurs when two consecutive actions in the trace are performed by the same thread.*

Let $CC(\delta)$ denote the number of context continuations in a trace δ , we have the following lemma:

Lemma 1. *Minimizing $CS(\delta)$ is equivalent to maximizing $CC(\delta)$.*

Proof. Traversing the trace once, it is easy to see that for each action, either $CS(\delta)$ or $CC(\delta)$ is incremented. Thus, $CS(\delta) + CC(\delta) = N - 1$. Hence, $CS(\delta)$ is minimized when $CC(\delta)$ is maximized.

Therefore, our goal becomes to maximize the number of context continuations in the simplified trace. Now let us consider the action sequence represented by each node in the dependence graph. Since all actions in the same action sequence are performed by the same thread, their number of context continuations are already optimized. The remaining possible context continuations can only come from actions that are in different action sequences. Mapping this back to the dependence graph and because nodes representing action sequences by the same thread are connected by local edges, we have the following lemma:

Lemma 2. *Minimizing $CS(\delta)$ is equivalent to maximizing the number of context continuations contributed by local edges in the dependence graph.*

Consider a local edge in the graph, if the action sequences represented by the two nodes connected by this local edge are consolidated together, it will contribute one context continuation. Let us call a *merging* operation as the consolidating of two nodes connected by a local edge in the dependence graph. As each merging operation eliminates a local edge and correspondingly reduces one node in the dependence graph, it is easy for us to get the following theorem:

Theorem 2. *Minimizing $CS(\delta)$ is equivalent to minimizing the number of nodes in the dependence graph.*

Following Theorem 2, to produce an optimal solution, our objective is performing as many merging operation as possible to minimize the number of nodes in the dependence graph. However, recall that the dependence relation between actions in the trace must be respected. Therefore, we cannot arbitrarily perform the merging operation without satisfying a certain pre-condition: the merging condition is that the to-be-merged two nodes are connected by the local edge only. Otherwise, the resultant graph after the merging operation would become cyclic that violates the definition of dependence graph. Mapping this back to the semantics of the dependence relation, the merging condition simply requires that there should not exist another dependent action in the trace that interleaves the two action sequences represented by the to-be-merged two nodes in the dependence graph. Checking the merging condition is simple because it only requires testing the reachability relation between the two merged nodes, which costs a linear running time in the number of nodes in the dependence graph.

Therefore, our dependence graph simplification algorithm (Algorithm 2) traverses each local edge in the dependence graph, and performs the merging operation if the merging condition is satisfied. This algorithm evaluates each local edge in the initial dependence graph once and each evaluation computes the reachability relation between two nodes once. The worst case time complexity is thus quadratic in the number of nodes in the initial dependence graph.

Algorithm 2 SimplifyDependenceGraph(*graph*)

```

1: input: graph (the dependence graph)
2: output: graph' (the simplified dependence graph)
3: graph'  $\leftarrow$  graph
4: for each local edge nodea  $\rightarrow$  nodeb in a random order do
5:   if nodeb is not reachable from nodea except from the local edge then
6:     merge(nodea, nodeb, graph')
7:   end if
8: end for

```

Notice that in our merging algorithm, the evaluation order of the local edges may affect the simplification result. To illustrate this problem, let us take the (incomplete) dependence graph in Figure 1 as an example. The graph contains 6 nodes, 3 local edges (denoted by dashed arrows \dashrightarrow), and 4 remote edge (denoted by solid arrows \rightarrow): $a_1 \dashrightarrow a_2$, $b_1 \dashrightarrow b_2$, $c_1 \dashrightarrow c_2$, $a_1 \rightarrow b_2$, $c_1 \rightarrow b_2$, $b_1 \rightarrow a_2$ and $b_1 \rightarrow c_2$. If b_1 and b_2 are merged first, as shown in Figure 1 (a), it would produce the trace $\langle a_1-c_1-b_1-b_2-c_2-a_2 \rangle$ that contains 4 context switches. However, the optimal solution is to merge a_1 and a_2 , and c_1 and c_2 , which produces the trace $\langle b_1-a_1-a_2-c_1-c_2-b_2 \rangle$ that contains only 3 context switches. In fact, this problem is NP-hard (proved by Jalbert and Sen [13]), and there does not seem to exist an efficient algorithm for generating an optimal solution. Our algorithm thus picks a random order (or any arbitrary order) for evaluating the local edges. Though

it does not guarantee to produce a global optimum, it always produces a local optimum specific to the chosen evaluation order.

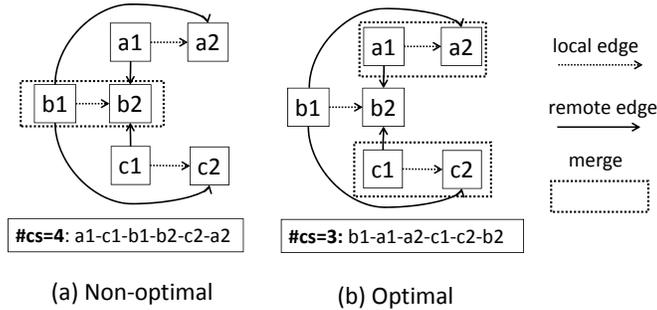


Fig. 1. A greedy merge may produce non-optimal result in (a). Unfortunately, the problem of producing the optimal result in (b) is NP-hard.

4 Implementation and Experiments

We have implemented *SimTrace* as a prototype tool on top of our *LEAP* [12] record and replay framework for multithreaded Java programs. From the user’s perspective, our tool consists of three phases. It first obtains a trace of a buggy concurrent Java program execution, which contains all the shared memory reads and writes as well as synchronization operations performed by each thread in the program. Then our tool applies the *SimTrace* algorithm on the trace and produces a simplified trace. In the third phase, it uses a replay engine to re-execute the program according to the scheduling decisions in the simplified trace. Our replayer is transparent to the programmers such that they can deterministically investigate the simplified buggy trace in a normal debugging environment.

The goal of our experiments is to investigate whether our approach is effective and how efficient it is in reducing the thread context switches in the trace. We chose eight widely used multithreaded Java benchmarks as the evaluation subjects (shown in the first column in Table 4). Each subject has one or more known concurrency bugs. *Philosopher* is a simulation of the classical dining philosophers problem, *Bubble* is a buggy multithreaded version of the bubble sort algorithm, *TSP* is a multithreaded implementation of a parallel branch and bound algorithm for the travelling salesman problem, *StringBuffer* is an open library from Sun’s JDK 1.4.2, *Cache4j* is a thread-safe implementation of cache for Java objects with an atomicity violation bug, *Weblech* is a multi-threaded web site download and mirror tool, *SpecJMS* is SPEC’s benchmark for evaluating the performance of enterprise message-oriented middleware servers based on JMS, and *Jigsaw* is W3C’s leading-edge web server platform.

Similar to *Tinertia* [13], we use the random testing approach to generate the initial buggy trace for each subject. For each trace, we ran *SimTrace* multiple times with different evaluation orders of the local edges during our graph merging process (Algorithm 2). To remove the non-determinism related to random numbers, we fix the seed of random numbers to a constant in all the subjects. All experiments were conducted on a HP EliteBook running Windows 7 with 2.53GHz Intel Core 2 Duo processor and 4GB memory. For others to verify our experimental results, we put our implementation and all the evaluation subjects publicly available at <http://www.cse.ust.hk/prism/simtrace>.

Program	LOC	Thread	SV	Trace Size	Time	Old Ctxt	New Ctxt	Reduction
Philosopher	81	6	1	131	6.0ms	51	18.0	65%
Bubble	417	26	25	1,493	23.0ms	454	163.0	71%
Elevator	514	4	13	2104	8.0ms	80	14.0	83%
TSP	709	5	234	636,499	149.0s	9272	1337.0	86%
Cache4j	3,897	4	5	1,225,167	592.0s	417	33.0	92%
Weblench	35,175	3	26	11,630	57.0ms	156	24.0	85%
OpenJMS	154,563	32	365	376,187	38.0s	96,643	11,402.0	88%
Jigsaw	381,348	10	126	19,074	130.0ms	2396	65.0	97%

Table 1. Experimental results. Data are averaged over 50 runs for each subject.

Table 4 shows the experimental results. All data are averaged over 50 runs. The first five columns show the statistics of the test cases, including the program name, the size of the program in lines of source code, the number of threads, the number of real shared memory locations that contain both read and write accesses from different threads in the given trace, and the length of the trace. The next four columns shows the statistics of our trace simplification algorithm (all on average), including the running time of our analysis, the number of context switches in the original trace, the number of context switches in the simplified trace and the percentage of reduction due to our simplification. The results show that our approach is promising in terms of both the trace simplification efficiency and the effectiveness. For the eight subjects, our approach is able to reduce the number of context switches in the trace by 65% to 97% on average. This reduction percentage is close to that of *Tinertia*, the reduction percentage of which ranges from to 32.1% to 97.0% in their experiments. More importantly, our approach is able to scale to much larger traces compared to that of *Tinertia*. For a trace with only 1505 events (which is the largest trace reported by *Tinertia* in their experiments), *Tinertia* requires a total of 769.3s to finish the simplification, while our approach can analyze a trace (the *Cache4j* subject) with more than 1M events within 600s. For a trace (the *Bubble* subject) with 1,493 events, our approach requires only 23ms to simplify it. Although a direct comparison between *Tinertia* and our approach is not applicable as we two approaches are implemented for different program languages (*Tinertia* is implemented for C/C++

programs) and we have different evaluation subjects, we believe the statistical data provides some evidence demonstrating the value of our approach compared to the state of the art.

5 Related Work

From the perspective of the trace theory, our dependence graph modeling of traces is an instantiation of Mazurkiewicz traces [1], which models a class of equivalent traces with respect to an alphabet and a dependence relation over the alphabet. Different from the equivalence axiom of Mazurkiewicz traces [1], our trace equivalence theorem is built on top of the computation equivalence of program state transitions and relies on a concrete model of the program execution semantics.

Our model of the dependence relation is closely related to, but different from the classical happens-before model [14] and various other causal models [3, 17, 20, 25], which do not enforce the conflicting orders used in our model, but rely on the value dependencies between the events to obtain a more precise causal model than ours. For example, Wang et al. [25] introduced a notion of guarded independence to enable precisely checking of atomicity violations, Chen et al. [3] proposed a notion of sliced causality that significantly reduces the size of the computed causality relation by slicing the causal dependences between the events, and Șerbănuță et al. [20] proposed a maximal causal model that comprises in theory all consistent executions that can be derived from a given trace. Although using a more precise dependence relation model may further reduce the context switches in the trace, as explained in Section 2.1, our strict modeling enables us to more efficiently perform the trace simplification.

Besides the problem of reducing the context switches in the trace, another important problem for the trace simplification is to reduce the size of trace. Along this direction, Tallam et al. [22] proposed an execution reduction (ER) system for removing the events that are irrelevant to the bug property in the trace. Similar to `SimTrace`, it also builds a dependence graph based on the dynamic dependencies between events in the trace. The main difference is that the ER system in [22] lacks a formal modeling of the trace elements. Without formalizing the semantics of each event in the trace, it is not obvious to understand the characteristics and the correctness of the resultant dependence graph.

To help locate the cause of the bug in an error trace, a number of software model checking algorithms [10, 9, 2] have been proposed to minimize an error trace and extract useful counterexamples when a bug is found. Delta Debugging [26] has also been extended to discover the minimal difference in thread scheduling necessary to produce a concurrency-based error [4]. The difference between our approach and this school of techniques is that our approach is based on reduction on a single trace, while they in spirit are based on comparing related executions, e.g., similar pairs of executions such that one of them satisfies the specification and the other does not.

To help with automatic concurrent program verification, Sinha and Wang [21] recently proposed a novel approach that separates intra- and inter-thread reasoning by symbolically encoding the shared memory accesses and composing the intra-thread summaries based on a sequential consistent memory model. Since this approach avoids redundant bi-modal reasoning, it has been shown to greatly improve the efficiency of trace analysis over previous approaches [24]. A promising way to go with this approach is to investigate how to apply it for helping programmers understand concurrency bugs.

6 Conclusion

We present an efficient static trace simplification technique for reducing the context switches in a concurrent program execution trace. By constructing a dependence graph model of events, our algorithm scales linearly to the trace size and quadratic to the number of nodes in the dependence graph. Moreover, underpinned by a trace equivalence theorem, our approach guarantees to generate an equivalent simplified trace without any dynamic program re-execution, making it attractive to practical use.

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7 Appendix: A Proof of Theorem 1

Proof. Let us say two actions are *equal iff* they perform the same operation on the same variable and also read and write the same value. The core of the proof is to prove the following lemma:

Lemma 3. *For any action α' in δ' , suppose it is the n^{th} action of thread t_i , then α' is equal to the n^{th} action of t_i in δ .*

If Lemma 3 holds, we can prove Theorem 1 by applying it to the last actions that write to each variable in both δ and δ' . To prove Lemma 3, we first define a notion of *version number* and show two lemmas related to it:

Definition 7. *Every variable is associated with a **version number** such that it is (1) initialized to be 0 and (2) incremented by 1 when the variable is written by an action.*

Lemma 4. *For any action α' in δ' , suppose it is the k^{th} action that writes to a variable s , then α' is also the k^{th} action that writes to s in δ .*

Proof. To prove Lemma 4, we only need to make sure the order of write actions on each variable is unchanged during the rescheduling of the trace from δ to δ' . This follows our modeling of the dependence relation includes all synchronization orders and the WRITE \rightarrow WRITE orders on the same variable. ■

Lemma 5. *For any action α' in δ' , suppose it reads the variable s with version number p , then α' also reads s with the same version number p in δ .*

Proof. Similar to the proof of Lemma 4, since our model of the dependence relation includes all the synchronization orders and the WRITE \rightarrow READ and READ \rightarrow WRITE orders on the same variable, we guarantee every READ action in the rescheduled trace reads the value written by the same WRITE action as that in the original trace. ■

Let $\sigma[s]^p$ denote the value of variable s with version number p , we next prove Lemma 3 by deduction on the version number of each variable:

Proof. Consider the j th actions performed by t_i , denoted by $\alpha_{i:j}$ and $\alpha'_{i:j}$ in δ and δ' respectively. To prove $\alpha'_{i:j}$ is equal to $\alpha_{i:j}$, we need to satisfy two conditions. First, their actions should be the same, i.e., they perform the same operation on the same variable. Second, suppose they both operate on the variable s (which should be true if the first condition holds), the values of s before $\alpha'_{i:j}$ is performed in δ' should be the same as that in δ before $\alpha_{i:j}$ is performed. Let $\pi_{i:j}$ and $\pi'_{i:j}$ denote the local store of t_i after $\alpha_{i:j}$ is performed in δ and after $\alpha'_{i:j}$ is performed in δ' , respectively. For the first condition, since the execution semantics determine that the next action of any thread is determined by that thread's current local store, we need to ensure (I) $\pi'_{i:j-1} = \pi_{i:j-1}$. For the second condition, suppose $\alpha_{i:j}$ and $\alpha'_{i:j}$ operate on s with version number p and p' , respectively, we need to ensure (II) $\sigma'[s]^{p'} = \sigma[s]^p$.

Let's first assume Condition I holds, we prove $p' = p$ in Condition II. If $\alpha'_{i:j}$ writes to s , i.e., $\alpha'_{i:j}$ is the p'^{th} action that writes to s , by Lemma 4, we can get that the corresponding action of $\alpha'_{i:j}$ in δ is also the p'^{th} action that writes to s . As Condition I holds, we know $\alpha_{i:j}$ is the corresponding action of $\alpha'_{i:j}$ in δ' . Since $\alpha_{i:j}$ operates on s with version number p in our assumption, we get $p' = p$. Otherwise if $\alpha'_{i:j}$ reads on s , by Lemma 5, we can get that $\alpha'_{i:j}$'s corresponding action in δ also reads s with the same version number, and similarly, we get $p' = p$.

We next prove both Condition I and Condition II hold. For condition I, suppose $\alpha_{i:j-1}$ and $\alpha'_{i:j-1}$ operate on the variable $s1$ with version number $p1$. To satisfy condition I, we need again to make sure (Ia) $\pi'_{i:j-2} = \pi_{i:j-2}$ and (Ib) $\sigma'[s1]^{p1} = \sigma[s1]^{p1}$. For condition II, let $\alpha_{i1:j1}$ and $\alpha'_{i1':j1'}$ denote the actions that write $\sigma[s]^p$ and $\sigma'[s]^{p'}$, respectively. Since the current value of a variable is determined by the action that last writes to it, to satisfy condition II, we need to make sure $\alpha'_{i1':j1'}$ is equal to $\alpha_{i1:j1}$, which again requires (IIa) $\pi'_{i1':j1'-1} = \pi_{i1:j1-1}$ and (IIb) $\sigma'[s]^{p'-1} = \sigma[s]^{p-1}$. If we apply this reasoning logic deductively for all threads, we will finally reach the base condition (i) $\forall t_i \in \mathbb{T}, \pi'_{i:0} = \pi_{i:0}$ and

(ii) $\forall s \in \mathbb{S}, \sigma'[s]^0 = \sigma[s]^0$, which are satisfied by the equivalence of the initial program states $\Sigma'^0 = \Sigma^0$. Hence, Lemma 3 is proved.

Therefore, Theorem 1 is proved. ■